PREPRINT UCRL- 77820

Lawrence Livermore Laboratory

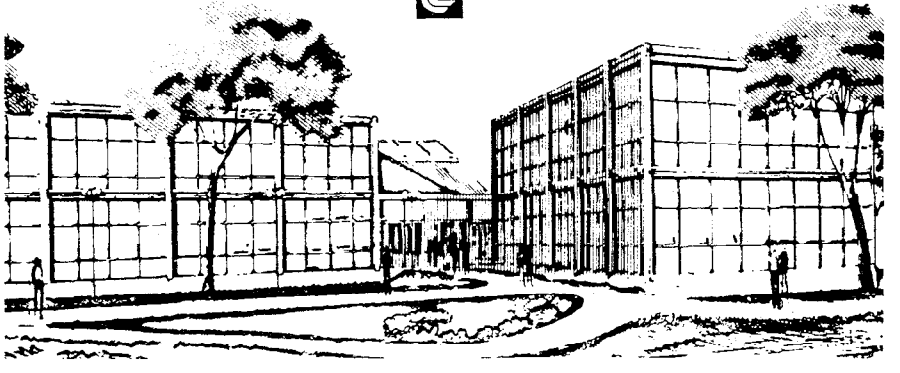
NECESSARY CONDITIONS FOR THE INITIATION AND PROPAGATION OF NUCLEAR DETONATION WAVES IN PLANE ATMOSPHERES*

Thomas A. Weaver and Lowell Wood

March 7, 1977

This paper was prepared for submission to Physical Review A.

This is a preprint of a paper intended for publication in a journal or proceedings. Since changes may be made before publication, this preprint is made available with the understanding that it will not be cited or reproduced without the permission of the author.



DISCLAIMER

This document was prepared as an account of work sponsored by an agency of the United States Government. Neither the United States Government nor the University of California nor any of their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness, or usefulness of any information, apparatus, product, or process disclosed, or represents that its use would not infringe privately owned rights. Reference herein to any specific commercial product, process, or service by trade name, trademark, manufacturer, or otherwise, does not necessarily constitute or imply its endorsement, recommendation, or favoring by the United States Government or the University of California. The views and opinions of authors expressed herein do not necessarily state or reflect those of the United States Government or the University of California, and shall not be used for advertising or product endorsement purposes.

NECESSARY CONDITIONS FOR THE INITIATION AND PROPAGATION OF NUCLEAR DETONATION WAVES IN PLANE ATMOSPHERES*

Thomas A. Weaver and Lowell Wood

University of California Lawrence Livermore Laboratory
Livermore, California 94550

ABSTRACT

The basic conditions for the initiation of a nuclear detonation wave in an atmosphere having plane symmetry (e.g. a thin, layered fluid envelope on a planet or star) are developed. Two classes of such a detonation are identified: those in which the temperature of the plasma is comparable to that of the electromagnetic radiation permeating it, and those in which the temperature of the plasma is much higher. Necessary conditions are developed for the propagation of such detonation waves for an arbitrarily great distance. The contribution of fusion chain reactions to these processes is evaluated. By means of these considerations, it is shown that neither the atmosphere nor oceans of the Earth may be made to undergo propagating nuclear detonation under any circumstances.

*Research performed under the auspices of the U.S. ERDA under contract W-7405-ENG-48.

I. INTRODUCTION

The possibility that a nuclear explosion might trigger the nuclear detonation of the atmosphere or oceans of the Earth has been seriously investigated on several occasions since 1943.[1,2,3] Despite resolving all physical uncertainties in such a way as to favor a detonation, these investigations all reached the conclusion that such a detonation is impossible.

The present paper reviews and extends these previous studies by deriving the general necessary conditions for the initiation and propagation of nuclear detonation waves in plane atmospheres or layered fluids, taking into account the great advances in theoretical, experimental, and computational physics that have been made in the interim. As we shall see, the effect of these advances is to reduce the physical uncertainties in such a way as to preclude the detonation of the atmosphere or oceans by an even greater margin.

The next section deals with the general characteristics and types of nuclear detonation waves, while Section III treats the needed nuclear cross-sections. Sections IV, V, and VI give detailed conditions for the existence of non-equilibrium, equilibrium, and fusion-chain-mediated nuclear detonation waves respectively, and further show that such conditions cannot be met in the Earth's atmosphere. Section VII describes detailed computer calculations which lead to the same conclusion. Section VIII treats nuclear detonation waves in an oceanic environment, and demonstrates their impossibility for the case of the Earth. Finally, Section IX summarizes our principal conclusions.

II. GENERAL CHARACTERISTICS OF NUCLEAR DETONATION WAVES

A nuclear detonation wave is basically a shock wave which has its energy and propagation velocity maintained against hydrodynamic and heat conduction losses by nuclear reactions occurring within the wave. Most dominant features of the power flow in a nuclear detonation wave bear a direct analogy to those encountered in chemical detonation wave theory[4,5]. Such a wave rapidly reaches a steady state configuration in its co-moving frame in which the locally deposited reaction energy flows in a time-stationary fashion into doing hydrodynamic work on the material both ahead and behind the wave (thereby shock heating and compressing the material ahead of the wave, due to its relatively much lower temperature and pressure), and into internal energy of the immediately post-shock material, from which it flows by radiative and electronic thermal conduction into all cooler portions of the material, both pre-shock and further post-shock. Nuclear detonation waves have been studied previously in connection with supernovae explosions[6-8] and laser-induced fusion[9-13].

Sufficient conditions for the propagation of a self-sustaining detonation depend on the precise nature of the interactions between the plasma components, and are discussed in a general way by Zel'dovich and Kompaneets.[5] Two necessary conditions that follow from conservation of energy and momentum are:

$$\dot{E}_N > \dot{E}_{Rad} \quad \text{(ignition condition)} \tag{1}$$

over some portion of the wave, and that:*

*Here we have assumed the internal energy of the wave is large compared to the ambient internal energy of the unshocked fuel.

$$\rho E_{Nl} > E_{int} \quad \text{(breakeven condition)} \tag{2}$$

where $\dot{E}_N$ is the rate of nuclear energy generation per unit volume, $\dot{E}_{Rad}$ is the rate of radiative energy loss per unit volume, E_{Nl} is the total nuclear energy generated per gram of material, and E_{int} and ρ are the internal energy density and matter density respectively, measured at a common point in the detonation.

The most striking difference between chemical and nuclear detonation waves is that the latter generate $\sim 10^7$ times more energy per gram of fuel, resulting in typical nuclear detonation wave velocities of several thousand kilometers per second, compared with a few kilometers per second for the chemical case.

If no radiation were present, a nuclear detonation wave would also be $\sim 10^7$ times hotter than a chemical wave (i.e. kT $\sim$ 3 MeV vs. 1/3 eV). In general, however, the enormous heat capacity of the radiation field at these high temperatures serves to greatly limit the temperatures actually attained in nuclear detonation waves. In particular, if the radiation field is in thermal equilibrium with the detonating material, the temperature, T, and the internal energy, E_{int}, are related by (neglecting relativistic electron effects):

$$aT^4 + \frac{3}{2}\frac{\rho N_A\, kT}{\bar{A}} = E_{int} \tag{3}$$

where $a = 7.56 \times 10^{-15}$ erg/cm^3/°K^4 is the radiation energy density constant, N_A is Avogadro's number, $\bar{A}$ is the mean atomic number for all plasma components including electrons, and k is Boltzmann's constant. For a typical internal energy corresponding to 1 MeV per nucleon, we find kT = 1.6 keV for $\rho = 10^{-3}$ g/cm^3, and kT = 9.2 keV for ρ = 1 g/cm^3.

The degree of radiative equilibration, and thus the temperature of the detonation is determined by the optical thickness of the detonating region and the time available for radiation to be emitted and thermalized as the wave sweeps over a given element of matter. The principal radiative processes involved are bremsstrahlung[14], which provides direct radiative cooling, and inverse Compton scattering,[15] which for sufficiently great optical thicknesses can greatly magnify the effect of bremsstrahlung cooling by up-scattering the low energy photons it produces at the expense of electron thermal energy. The question of radiative equilibration within a shock wave has been extensively studied in astrophysics with regard to supernova shock waves[16-17] and neutron star accretion[18,19], as well as by Konopinski, et al.[1] It is found in these studies that for phenomena whose specific energy is $\sim$1 MeV per nucleon, that 10-100 (typically 30) Compton scattering events (per low energy bremsstrahlung photon) are required to bring the radiation field into approximate energy equilibrium with the electrons (also see ref. 10).

Most of the detonation waves studied to date in astrophysics[6-8] have involved very optically thick systems which consequently attain full radiative equilibrium, and experience essentially no radiative losses in the sense of eq. (1). Detonation waves studied in laser-induced microexplosions[9-13], on the other hand have generally involved relatively optically thin pellets in which the radiation field is so far from equilibrium that only a small fraction of the pellet's internal energy resides in radiation. For detonations to propagate in such (non-equilibrium) circumstances, the rate of nuclear energy generation must exceed the <u>total</u> rate at which energy is being radiated by the plasma by an amount sufficient to make up hydrodynamic and particle heat conduction losses.

For cases of intermediate optical thickness, such as the planetary and stellar atmospheres of present interest, one must consider necessary conditions for the existence of detonation waves in both equilibrium and non-equilibrium cases. This is undertaken in the following sections.

III. NUCLEAR CROSS SECTIONS

On the basis of the large number of quantitative nuclear cross section measurements that have been made over the past four decades, theoretical and empirical models[20-22] have been developed that are capable of accurately predicting and/or fitting such cross sections over a wide range of nuclei and reaction types. In particular, these models are directly applicable to the nuclear reactions that have been implicated in the possible detonation of the Earth's atmosphere or ocean by nuclear bomb explosions. Using these models, the total cross section, $\sigma_{12}(E)$, for the reaction of nuclei of types 1 and 2 can be expressed in the form:[22]

$$\sigma_{12}(E) = \frac{S\, e^{-2\pi\eta}}{E} \quad \text{barns} \tag{4}$$

where E is the center-of-mass energy of the two colliding particles in MeV, S is the reaction strength factor in MeV-barns, which is approximately independent of energy and is given by:

$$S = \kappa \frac{Z_1 Z_2}{\sqrt{A}} \exp(2X - \alpha E) \tag{5}$$

and $e^{-2\pi\eta}$ is the factor by which the reaction strength is reduced by the necessity for the nuclei to penetrate their mutual Coulomb barriers. The

terms in these equations are defined by:

$$\alpha = 0.1215 \sqrt{\frac{AR^3}{Z_1 Z_2}} \ \text{MeV}^{-1} \tag{6}$$

$$X = 0.52495 \sqrt{AZ_1 Z_2 R} \tag{7}$$

$$\eta = 0.15748 \, Z_1 Z_2 \sqrt{\frac{A}{E}} \tag{8}$$

$$A = \frac{A_1 A_2}{A_1 + A_2} \tag{9}$$

Here A_1 and A_2, and Z_1 and Z_2, are the atomic weight and number of nuclei 1 and 2 respectively, R is the nuclear interaction radius in fermi, and κ is the reflectivity factor. The advantage of expressing σ_{12} in this form is that the unspecified parameters are either explicitly energy-independent (in the case of the interaction radius) or become so when averaged over reaction resonances (in the case of the reflectivity factor). For reactions in which the intermediate compound nucleus formed has $(A_1 + A_2) > 20$ and an excitation energy of $\gtrsim$ 3 MeV, so many relatively closely spaced resonances exist that they can be successfully treated statistically.[22] For the case when σ_{12} is taken to be the resonance-averaged total cross section for <u>all</u> nuclear reactions involving compound nucleus formation (including nuclear elastic scattering), such a statistical treatment gives:[22]

$$\kappa = \begin{cases} 0.20 & \text{for proton-induced reactions} \\ 0.32 & \text{for alpha-induced reactions} \\ 0.16 & \text{for neutron-induced reactions} \end{cases} \qquad (10)$$

$$R = \begin{cases} 1.25\ A_1^{1/3} + 0.1 & \text{for n- or p-induced reactions} \\ 1.09\ A_1^{1/3} + 0.7 & \text{for } \alpha\text{-induced reactions} \end{cases}$$

The resulting total cross sections (calculated by use of Eq. (4)) are found to be accurate to within about a factor of two when compared with experimental measurements.

The assumptions involved for Eqs. (4)-(10) become invalid for non-neutron-induced reactions when:

$$E \gtrsim E_c \equiv \frac{1.44\ Z_1 Z_2}{R}\ \text{MeV} \qquad (11)$$

where E_c is the Coulomb barrier energy for the reaction. In such cases, an upper limit on $\sigma_{12}(E)$ is the larger of πR^2, the geometric cross section of the interacting nuclei, and $\pi\lambda\!\!\!^{-2}$, the maximum s-wave resonant cross section, where $\lambda\!\!\!^{-}$ is the de Broglie wavelength of the interacting system ($\pi\lambda\!\!\!^{-2} = 0.6566/AE$ barns).

In discussing the prospects for atmospheric ignition, the nuclear reactions for which detailed nuclear cross sections will be required are $^{14}N + {}^{14}N$ reactions yielding charged particles, $^{14}N(\alpha,p)^{17}O$, and $^{11}B(p,2\alpha)^4He$. The existing experimental cross section measurements[23] for $^{14}N + {}^{14}N$ fusion reactions cover the lab energy range of 9.4 to 22 MeV and are plotted in Fig. 1. It is apparent the cross section is insignificant for lab energies below 10 MeV, due to Coulomb repulsion, but rises rapidly to a near-geometric cross section of $\sim$1 barn above 20 MeV. No resonances in the fusion cross section

are seen to occur, as expected from the large number of closely spaced, overlapping energy levels in the intermediate $^{28}Si^*$ compound nucleus. The $^{14}N + {}^{14}N$ fusion reactions were found to be dominated by the three-product reactions $^{14}N(^{14}N,2\alpha)^{20}Ne$, $^{14}N(^{14}N,2p)^{26}Mg$, $^{14}N(^{14}N,\alpha p)^{23}Na$, and $^{14}N(^{14}N,pn)^{26}Al$ which are exothermic by 7.92, 7.36, 5.54, and 2.58 MeV respectively. No significant number of two-product reactions (e.g. $^{14}N(^{14}N,\alpha)^{24}Mg$) were observed; and indeed, such reactions are believed to constitute $\lesssim$10% of the ^{14}N fusion reactions, due to their small statistical weights relative to three-product reactions when the very highly excited nature of the intermediate $^{28}Si^*$ nucleus is taken into account.

Due to its lack of resonant structure, the $^{14}N + {}^{14}N$ fusion cross section can be well-fitted by the statistical formalism outlined above. In particular, the low energy behavior of the cross section can be determined from Eqs. (4)-(9) by fitting κ and R to the existing data yielding $\kappa \simeq 0.03$ and $R \simeq 8.01$ fermi. The high energy behavior can be extrapolated using the parametrization of Wong[24] in the form:

$$\sigma(E) = \frac{R^2\hbar\omega_o}{2E}\,\ell n\{1 + \exp[2\pi(E-E_o)/\hbar\omega_o]\} \qquad (12)$$

with $\hbar\omega_o = 2.96$ MeV and $E_o = 8.25$ MeV. Equation (12) is believed accurate to $\pm$30%,[24] up to a center-of-mass energy of 40 MeV, where direct spallation reactions instead of compound nuclear reactions become dominant.

The cross section for the $^{14}N(\alpha,p)^{17}O$ reaction has been measured by several groups of experimenters,[25-27] and a compilation of the results is given in Fig. 2, labelled σ_{EXPT}. The results of the statistical theory for R and κ given by Eq. (10) for $\alpha + {}^{14}N$ compound nucleus formation (R = 3.33 fermi, κ = 0.32) are found to give a reasonable fit to the experimental

cross section, when an average over the many narrow resonances is taken. This statistical cross section is thus adopted for use below, with the geometric cutoff at $\pi R^2 = 0.35$ barns, and is plotted as σ_{ADPT} in Fig. 3.

The cross section for the $^{11}B(p,2\alpha)^4He$ reaction is now well-known[28] and is plotted in Fig. 5. (See Section VI)

The cross sections for the nuclear reactions potentially involved in ocean burning (i.e. the various reactions of hydrogen and oxygen isotopes) are well-known because of their role in hydrogen burning in stars. Convenient representations of their thermal distribution-averaged cross sections, $\langle\sigma v\rangle$'s, are given in Ref. 21.

IV. RADIATIVE CONSTRAINTS ON NON-EQUILIBRIUM NUCLEAR DETONATIONS

Since the temperature of the ions in a non-equilibrium nuclear detonation greatly exceeds that of the radiation field, energy transferred to radiation is very unlikely to be transferred back to the ions (via the electrons), and can therefore be regarded as lost. The ignition criteria (Eq. 1) can then be recast to give a lower limit on the nuclear energy generation rate required for ignition at a given ion temperature in terms of the total radiative energy emission rate. Because the relative importance of the inverse Compton effect depends critically on the optical depth of the igniting region, it is convenient to first consider the less stringent lower limit obtained by ignoring photon up-scattering by the hotter electrons and including only the energy loss due directly to bremsstrahlung radiation.[14]

The nuclear reaction reaction rate, $\dot{E}_N$, may be written as (c.f. ref. 29):

$$\dot{E}_N = \frac{n_1 n_2}{1 + \delta_{12}} \langle\sigma v\rangle Q, \tag{13}$$

where, as usual, n_1 and n_2 are the number densities of the reacting species; δ_{12} is 1 if the reactants are identical and 0 otherwise; $\langle\sigma v\rangle$ is the velocity distribution average of the product of the relative thermal velocity, v, of two potentially reacting ions and the reaction cross section at that velocity, σ; and Q is the reaction energy. To further favor ignition, we will assume that all reaction products deposit their energy in the ions. We shall also assume here that this deposition takes place locally and instantaneously and that the ion distribution can be characterized by a temperature, T_i. The possible effects of non-thermal ions are considered in Section VI.

The bremsstrahlung radiation rate, $\dot{E}_{brem}$, may be written as[30]

$$\dot{E}_{brem} = 3.32\times10^{-15}\, g(T_e)\, T_e^{1/2}\, n_e n_i\, Z_1^2 \text{ keV/sec/cm}^3 \qquad (14)$$

Here n_e and n_i are the electron and <u>total</u> ion number densities, respectively, in cm^{-3}; T_e is the electron temperature in keV; $g(T_e)$ is a monotone, slowly increasing function, lowered-bounded by unity, which accounts for the relativistic increase of radiation emission[14,17] as the average thermal electron energy becomes non-negligible compared to the rest energy of an electron, and

$$Z_1^2 = \frac{1}{n_i} \sum_{\substack{\text{all ionic} \\ \text{species}}} n_j Z_j^2 \qquad (15)$$

where n_j and Z_j are the number density and atomic number of ion species j.

To relate T_i and T_e, we note that the energy flow from the ions to the electrons is given by[30]

$$\dot{E}_{i\to e} = 1.51\times10^{-13}(T_i - T_e)\frac{Z_0^2}{A_0} n_i n_e R_s(\ell n\Lambda_s - \tfrac{1}{2}) T_e^{-3/2} \text{ keV/sec/cm}^3, \qquad (16)$$

$$R_s \simeq 0.96\,[1+0.0004T_e\,(1+0.0045T_e)] \quad \text{for} \quad \begin{cases} T_e \lesssim 300 \text{ keV} \\ n_e \sim 10^{20} \text{ cm}^{-3} \end{cases} \qquad (17)$$

where T_i and T_e are in keV; $\ell n\Lambda_s$ is the usual Spitzer Coulomb logarithm including the quantum mechanical correction;[30] R_s is a correction factor for ion screening and relativistic electron effects;[31] and:

$$\frac{Z_0^2}{A_0} \equiv \frac{1}{n_i} \sum_{\substack{\text{all ionic} \\ \text{species}}} \frac{n_j Z_j^2}{A_j} \,. \qquad (18)$$

where A_j is the atomic weight of ion species j. The electron and ion temperatures are initially the same and diverge under the influence of nuclear heating and radiative cooling until the ion-electron energy transfer rate just balances bremsstrahlung losses, yielding the steady state relation:

$$T_i = T_e + \left(\frac{T_e}{6.74}\right)^2 \xi(T_e) \text{ keV} \qquad (19)$$

where, for convenience, we have defined:

$$\xi(T_e) = \frac{g(T_e)Z_1^2}{R_s(\ell n\Lambda_s - \frac{1}{2})}\left(\frac{A_0}{Z_0^2}\right) \qquad (20)$$

Solving for T_e, we find

$$T_e = \frac{-1 + \sqrt{1+4CT_i}}{2C} \,, \qquad (21)$$

where $C = 2.20\times10^{-2}\, \xi(T_e)$ keV^{-1}. In the physically interesting limit of $4CT_i \gg 1$, we have

$$T_e \simeq \left(\frac{T_i}{C}\right)^{1/2} = \left(\frac{45.5\, T_i}{\xi(T_e)}\right)^{1/2} \qquad (22)$$

Thus, from (14) we find

$$\dot{E}_{Brem} \simeq 8.62\times10^{-15}\, n_e n_i\, g(T_e)\xi^{-1/4}\, Z_1^2 \text{ keV/sec/cm}^3 \qquad (23)$$

Then, in order that $\dot{E}_N > \dot{E}_{brem}$ (the <u>minimal</u> necessary requirement for the

detonation to generate more thermonuclear power than it loses to radiation), we must have:

$$Q^* \langle\sigma v\rangle > 4.85\times10^{-17}\left[\frac{1+\delta_{12}}{n_1 n_2} n_i n_e\right] g(T_e)\, \xi^{-1/4} T_i^{*1/4} Z_1^2 \qquad (24)$$

where Q^* and T_i^* are Q and T_i in MeV, $\langle\sigma v\rangle$ is in cm^3/sec, and as before, number densities are in cm^{-3}.

For the sea level atmosphere with normal composition and standard temperature (STP), $Z_0^2/A_0 \simeq 3.6$, $Z_1^2 \simeq 53$, $n_i = 2.69\times10^{19}\ cm^{-3}$, $n_e/n_i \simeq 7.2$, and $n_{^{14}N}/n_i \simeq 0.8$. Under these conditions, criterion (24) for $^{14}N + {}^{14}N$ reactions becomes:

$$Q^* \langle\sigma v\rangle > 5.8\times10^{-14}\ g(T_e)\, \xi^{-1/4} T_i^{*1/4} \qquad (25)$$

where $g(T_e)\xi^{-1/4}$ is a factor of order unity which is plotted in Figure 3 along with $g(T_e)$, R_s, $\ell n\Lambda_s/15$, and $T_i/10T_e$ (for the exact solution (21)).

From Section III, we note that the most energetic of the dominant three-product $^{14}N + {}^{14}N$ fusion reactions is:

$$^{14}N + {}^{14}N \rightarrow {}^{28}Si^* \rightarrow {}^{20}Ne + \alpha + \alpha + 7.92\ MeV \qquad (26)$$

and thus we can take 7.92 MeV as an upper limit on the Q-value for ^{14}N fusion. This upper limit becomes a substantial overestimate for $^{14}N + {}^{14}N$ center-of-mass energies above 10 MeV, due to the increasing fraction of endothermic fusion and spallation reactions. In addition, many of the products are formed in excited states that emit γ-rays and thus represent a source of radiative energy loss.[23] Subsequent reactions between ^{14}N nuclei

and the α, p, and n fusion reaction products may slightly increase the net Q-value for ^{14}N fusion. However, over the time scale involved in radiative cooling at atmospheric density ($<10^{-5}$ sec), such reactions are either rare, endothermic, or both. (The effect of fusion chains is treated in Sections VI and VII and is also found to be insignificant). Reactions involving minor atmospheric constituents (e.g. oxygen and argon) are required by criterion (25) to have cross sections much greater than 10 barns in order to cause a detonation, due to the large ratio of radiating to reacting particles. Such large cross sections have never been observed for <u>any</u> nuclear reaction involving charged nuclei, the largest being 5 barns for the peak of the 107 keV resonance of the $(DT \rightarrow n\alpha)$ reaction. Thus it suffices to consider whether reaction (26) can cause a non-equilibrium detonation of the atmosphere.

The energy generation rate due to reaction (26) based on the cross sections of Fig. 1 is plotted in Fig. 4 together with the energy losses due to bremsstrahlung. By criterion (2), the maximum temperature, $T_{i,max}$, which the ions can reach in steady state with the electrons if all the nitrogen is burned is 853 keV (corresponding to an electron temperature of 139 keV). At this temperature, radiation losses exceed nuclear energy generation by a factor of 7×10^4. At lower ion temperatures this factor becomes astronomically large. Thus, by criterion (1) a non-equilibrium nuclear detonation wave is not possible in the terrestrial atmosphere.

It is interesting to note that electron-ion bremsstrahlung radiative energy losses, which scale as Z^3 on a per ion basis, are so much greater for the atmosphere than for a DT plasma that even if nitrogen had the same effective $Q\langle\sigma v\rangle$ as DT, the best nuclear fuel known, burning in an

optically- (and thus neutron-) thin configuration, it would still fail by more than a factor of 5 to satisfy the minimal detonation criterion (25).

Moreover, these optimistic considerations have ignored the huge hydrodynamic and thermal conduction losses inevitably associated with non-equilibrium thermonuclear detonations, as well as inverse Compton scattering losses, which greatly multiply the effect of bremsstrahlung losses in all but absolutely optically thin detonations. Moderate estimates of the combined effects of these factors indicate that the minimum "safety factor" of 7×10^4 precluding the non-equilibrium nuclear detonation of the atmosphere (noted above) should be increased to $10^6 - 10^7$.

V. EQUILIBRIUM NUCLEAR DETONATIONS

As was discussed in Section II, the radiation field in an optically thick nuclear detonation wave will typically be in near-equilibrium with the electrons after an average photon has undergone about 30 Compton scatterings within the hot, burning region. An average photon will diffuse out of the wave during this number of scatterings unless the half width, ℓ, of the wave exceeds $\sim \sqrt{30} \simeq$ 5-6 Compton scattering lengths ($\equiv \frac{1}{n_e \sigma_c}$). This consideration sets a lower limit on the half-width of an equilibrium nuclear detonation wave. Since n_e/ρ is $\sim 3 \times 10^{23}$ electrons/gram for all light elements except H^1, H^3, and He^3, this half-width condition can be re-expressed as:

$$\rho\ell \equiv \frac{1}{2}\int_{WF} \rho(s)\, ds \gtrsim 25\text{-}30 \text{ g/cm}^2 \qquad (27)$$

where $\int_{WF} ds$ is a line integral through the detonation wave front, and ρ is the characteristic density of the wave front.

The temperature of the ionic component of the plasma in an equilibrium detonation is necessarily not greatly different from that of the electron component, except at extremely high matter densities ($> 10^4$ gm/cm^3) unlikely to be ever attainable outside of laser-induced fusion microexplosions[32] or stellar cores. Besides being coupled far more strongly to the electron component of the plasma by ion-electron coupling (see Eq. (16)) at the much lower electron temperatures ($\lesssim 10$ keV) which we have seen are characteristic of equilibrium detonations, the ions receive much less of the thermonuclear power arising from fusion reactions, since all the charged debris of such reactions also couple far more strongly to the much cooler electrons than in the non-equilibrium case, and deposit corresponding less of their energy in the ion

component of the plasma (see equations (34) and (35) in Section VI). Taken together these factors insure that $T_i \simeq T_e$ for all equilibrium nuclear detonations of current interest.

Since the reaction rate of essentially all fusion reactions (in particular see Figures 1 and 2) drops sharply with decreasing ion temperature (due to the relatively much stronger Coulomb repulsion between nuclei), the Q $\langle\sigma v\rangle$ product is very much lower in an equilibrium detonation than in a non-equilibrium detonation. This is more than balanced, however, by the elimination of radiation losses in radiative equilibrium. Thus, any nuclear fuel may be burned in radiative equilibrium, with an efficiency limited only by hydrodynamic losses associated with explosive disassembly of the burning fuel. Thus the sun is able to efficiently burn protons, despite their being ≃25 orders of magnitude less reactive than DT, although it could not do so without the hydrodynamic confinement supplied by gravity and the radiative confinement supplied by its huge optical thickness.

The condition for negligible radiative energy loss is that the energy-weighted diffusion velocity, v_γ, of a photon across the wave's half width be much less than velocity of the detonation wave with respect to the detonating material, which by the Chapman-Jouget relation[5] (in the absence of losses) is just equal to the final sound speed in the detonation products, c_s. This condition can thus be expressed in the form:

$$v_\gamma \sim \frac{4c}{3\kappa\rho\ell} \ll c_s \qquad (28)$$

where c is the speed of light, and κ is the total radiative opacity of the detonating material. The portion of κ due to Compton scattering is $\kappa_e \equiv \sigma_c\rho/n_e \simeq 0.2$ cm^2/g for the usual case of $n_e/\rho \simeq 3\times10^{23}$ electrons/gram

discussed above. For low Z plasmas and $T_e \gtrsim 1$ keV, Compton scattering is the dominant source of radiative opacity. Since the sound speed in an equilibrium detonation wave is typically 2-3x10^8 cm/sec (see Section II), the condition for radiation being trapped within detonation waves in low Z plasmas becomes:

$$\rho\ell \gg 650 \ \text{g/cm}^2. \qquad (29)$$

Equation (29) thus represents a necessary condition for the attainment of an equilibrium detonation, except for the unique case of DT, which burns sufficiently well at the low temperatures characteristic of equilibrium detonation waves to tolerate substantial radiation losses. The general ignition criteria for equilibrium nuclear detonation waves is still given by Eq.(1) with $\dot{E}_{Rad} = \vec{\nabla}\,(aT^4\vec{v}_\gamma) \sim \frac{acT^4}{\kappa\rho\ell^2}$, where T is the common plasma temperature and a is the equilibrium radiation density constant given in Section II.

The condition for hydrodynamic losses not to quench the detonation is that the characteristic nuclear burn time, t_{burn}, not be much greater than the hydrodynamic disassembly time, t_{hydro}. This can be written:

$$t_{burn} \simeq \frac{\hat{A}}{\rho\,\langle\sigma v\rangle\,N_A} \lesssim \frac{\ell}{c_s} \simeq t_{hydro} \qquad (30)$$

or

$$\frac{c_s\,\hat{A}}{\rho\ell\,\langle\sigma v\rangle\,N_A} \lesssim 1 \qquad (31)$$

where $\hat{A}$ is the plasma mass associated with one nucleus of the most abundant reactant species in the reaction of interest, in atomic mass units. An upper limit on the maximum temperature, T_{max}, and thus the maximum value of $\langle\sigma v\rangle/c_s$, can be found from equations (2) and (3) by optimistically assuming that all the nuclear fuel burns as it passes through the detonation wave. We may then re-write (3) above as:

$$T_{max} < \left(\frac{\rho Q'}{a}\right)^{1/4} \tag{32}$$

where Q' is the nuclear reaction energy available per unit mass of nuclear fuel. These results yield a minimum necessary value of ℓ that material of given density ρ must have to sustain an equilibrium nuclear detonation wave.

For the case of the Earth's atmosphere ($Q' \simeq 3\times10^{17}$ erg/g and $\rho \simeq 2\times10^{-3}$ g/cm^3, about twice the ambient atmosphere density[5]), we find $T_{max} < 1.4$ keV. The nuclear reaction rate, $\langle\sigma v\rangle$, for nitrogen-nitrogen reactions is so low at this temperature ($\sim 10^{-180}$ cm^3/sec) that even if all the nitrogen and oxygen in the universe were somehow to be assembled so that their density was that of the Earth's atmosphere, and the entire mixture heated to 1.4 keV and maintained in this condition, not one single nitrogen-nitrogen fusion reaction would take place in the lifetime of the universe! Consideration of minor atmospheric constituents does not appreciably improve the prospects for detonation. The Earth's atmosphere thus fails to support an equilibrium nuclear detonation by a literally astronomical margin at the nuclear reaction rate corresponding to the maximum temperature that could be attained if the atmosphere were to burn to completion.

VI. FUSION CHAIN REACTIONS

In discussing non-equilibrium detonation waves, we assumed that the ions had a thermal distribution. Jetter[33] and McNally[34,35] have suggested however, that the fusion products, which are generally produced with a much higher energy and nuclear reactivity than the rest of the plasma, may induce a significant number of nuclear reactions before they slow down, perhaps enough to lead to a diverging, non-thermal fusion chain reaction.

The principal constraints on such a chaining process are that the potentially reactive fusion products, termed "chain centers", will be so rapidly slowed by Coulomb friction with the ions or electrons that they will not have a significant chance to react, or that they will be absorbed by reactions which produce no new chain centers. These constraints can be expressed by requiring that

$$\nu f_E \prod_j \frac{\sigma_{Nj} n_{Nj}}{\sigma_{sj} n_{sj} + \sigma_{Aj} n_{Aj} + \sigma_{Nj} n_{Nj}} > 1 \tag{33}$$

for a chain reaction to occur. Here σ_{Nj} is the characteristic cross section for a chain-center producing reaction to occur; σ_{sj} and σ_{Aj} are the cross sections for a chain center to be stopped or absorbed, respectively; n_{Nj} is the number density of ions with which the chain centers may react to make new chain centers; n_{sj} and n_{Aj} are the effective number density of particles contributing to stopping or absorbing chain centers respectively; f_E is the average fraction of the chain centers that escape from the reacting region during a chain cycle, the subscript j refers to reaction step j of the chain; and ν is the factor by which the number of chain centers would be increased in the absence of losses per completed chain cycle. For the physically interesting

case when the chain centers move much faster than the background ions, but still much slower than the electrons, we have[30]

$$\sigma_{se} \simeq 547 \frac{1}{\sqrt{A_c}} \frac{Z_c^2}{E_c^{1/2}\ (\text{MeV})\ T_e^{3/2}} \left(\frac{\ell n \Lambda}{15}\right) \text{ barns} \qquad (34)$$

$$\sigma_{si}^{C} \cong 1.95 \frac{A_c}{A_i} \frac{Z_c^2\ Z_i^2}{E_c^2\ (\text{MeV})} \left(\frac{\ell n \Lambda}{15}\right) \text{ barns} \qquad (35)$$

where σ_{se} is the stopping cross section due to electron Coulomb drag and σ_{si}^{C} that due to ion Coulomb drag; A_c and A_i, and Z_c and Z_i, are the atomic weights and numbers of the chain centers and background ions respectively; E_c (MeV) is the energy of a chain center in MeV, and (as usual) T_e is in keV. In addition, there is a nuclear scattering contribution to the ion stopping cross section, σ_{si}^{N}, which, though quite variable, is typically ~ 1 barn. Since all measured cross sections for nuclear reactions between any two charged nuclei are $\lesssim 1$ barn, with the exception of the 5 barn resonance in the DT fusion reaction, equations (33)-(35) place severe constraints on the conditions under which fusion chains may propagate.

As a specific example, consider the fusion chain which McNally[35] considers the "most dangerous" with respect to the ignition of the atmosphere:

$$\alpha + {}^{14}N \rightarrow p + {}^{17}O - 1.2 \text{ MeV} \qquad (36)$$

$$\alpha + {}^{17}O \rightarrow n + {}^{20}Ne + 0.6 \text{ MeV} \qquad (37)$$

$$n + {}^{14}N \rightarrow \alpha + {}^{11}B - 0.15 \text{ MeV} \qquad (38)$$

$$p + {}^{11}B \rightarrow 3\alpha + 8.7 \text{ MeV} \qquad (39)$$

$$\text{Net} \quad 2\alpha + {}^{14}N + {}^{14}N \rightarrow 4\alpha + {}^{20}Ne + 7.9 \text{ MeV} \qquad (40)$$

The highest energy α produced in this chain has an energy of 3.9 MeV (plus about 2/3 of the center of mass energy involved in reaction (39)), while an average α has an energy of $\lesssim 2$ MeV. Conservatively taking $E_c = 5$ MeV, $\ell n \Lambda = 15$, and $n_N/n_s = 1$ (where both reaction centers and stopping particles are considered to be nitrogen nuclei), and ignoring stopping effects other than ion Coulomb drag, we find from (33) and (35) that a minimum necessary condition for the net reaction (40) (exceedingly generously considered as a one step fusion chain) to occur is: $\sigma_N > 4.4$ barns which, as noted above, is considerably greater than the largest non-DT charged-particle nuclear reaction cross section.

In addition, from (34) we see that unless $T_e \gg 23$ keV, stopping effects due to electron Coulomb drag will require σ_N to be even larger. For example, at $T_e = 1.4$ keV, the maximum temperature that could be involved in the equilibrium detonation of the atmosphere, σ_N would have to exceed 290 barns for a fusion chain reaction to propagate.

The considerations of Section III, however, preclude values of σ_N greater than 0.4 barns, and this is confirmed by existing experimental measurements (see Figure 3).

The fusion chain (36)-(40) is also ruled out by other independent arguments. First, the $p + B^{11}$ reaction (39) has been extensively studied because of its CTR interest,[36,37] and its cross section is now well-known.[28] Detailed computer-based simulation studies in which a beam of protons of optimal energy was injected into a very hot ($T_e \sim 50$ keV) ^{11}B plasma[37,38] resulted in the production of less than 15% as much energy by non-thermal nuclear reactions as was originally present in the proton beam. Thus reaction (39), the only appreciably exothermic reaction in the fusion chain, would in fact represent an energy sink for the non-thermal ions. This result is readily appreciated by comparing the pB^{11} nuclear reaction cross section to the Coulomb stopping

cross section for protons on nitrogen, as is done in Figure 5. It is apparent from these cross sections that the factor in Eq. (33) corresponding to reaction step (39) (termed a "per-step-loss" factor) will be at most 0.3 (even if $n_{^{11}B} \sim n_{^{14}N}$). Second, the well-known reaction:

$$n + {}^{14}N \rightarrow p + {}^{14}C + 0.6 \text{ MeV} \qquad (41)$$

competes with reaction (38), as does the nuclear elastic scattering of neutrons on ^{14}N. An upper limit on the per-step-loss factor for reaction (38) is $\simeq 0.5$ (cf. ref. 39). Similarly the per-step-loss factor for reaction (37) can be conservatively taken to less than 0.1 (cf. ref. 40 and Eq. (35), even assuming ^{17}O is as abundant as ^{14}N).

Combining these results, and noting $\nu = 2$ for fusion chain (36)-(40), we find that at most 1.5×10^{-3} of the effective chain centers present at the beginning of each fusion chain cycle will be present or have been replaced at its completion! Thus, this "chain" would die out exceedingly rapidly, even assuming it could be initiated by an external source of chain centers.

Likewise, no other fusion chain which has been proposed to be involved in atmospheric nuclear ignition comes at all close to diverging, even when very generous cross section estimates are used; rather all of them very rapidly "converge" to zero reaction rate.

We further note that in addition to satisfying the criterion (33), a fusion chain must either make up the radiation losses considered in Section IV, or face the exceedingly large electron stopping cross sections characteristic of relatively low temperature equilibrium detonations. Eq. (23) provides an approximate but nontheless very severe, criterion for a non-equilibrium fusion chain to exist if the thermally-averaged $\langle\sigma v\rangle$ is replaced

with an appropriate non-thermal distribution average, and T_i is replaced with $\frac{2}{3} E_c$. Also, since the Compton scattering $\langle\sigma v\rangle$ is always much greater than fusion chain $\langle\sigma v\rangle$'s, the radiation field in an optically thick medium will typically equilibrate before the chain has progressed more than a few generations, even with very optimistic assumptions about the nature of the chain.

Finally, we note that, as we have assumed above, the electrons should remain quite Maxwellian, since the energy-exchange coupling constant between electrons is $A_i/A_e \geq 1836$ times that between ions and electrons,[30] while the ion-electron temperature ratios involved are generally much smaller than this factor.

VII. PROSPECTS FOR THE NUCLEAR DETONATION OF THE ATMOSPHERE: DETAILED NUMERICAL CALCULATIONS

While the preceding analytical considerations preclude the ignition of the Earth's atmosphere under any circumstances, it is of some interest to further confirm this conclusion by means of detailed numerical calculations. Such calculations were made using the FOKN non-thermal nuclear burn computer code developed originally for laser fusion calculations by Lee, Zimmerman, and Wood,[41] and later extended by Scharlemann, Weaver, Zimmerman, and Chu[42]. In its present form, this code follows the time evolution of the energy distributions of the reactants and products explicitly, utilizing the Fokker-Planck approximation for low-angle Coulomb scattering, and transfer matrices for high-angle Coulomb, nuclear, and radiative processes. The treatment of both the distribution functions and the radiative emission rates is relativistically correct, and an infinite isotropic, homogeneous plasma is assumed. In addition, the slight differences between the $\ell n\Lambda$ terms involved in the Coulomb interaction between different particle species are taken into account. The effects of an injected particle source are modelled by adding particles at a specified rate to a given energy group. Exponential number loss rates of one or more particle species can also be specified. This code is thus well suited to evaluate the possibility of non-equilibrium and fusion chain nuclear detonation modes. Indeed, the major simplifications inherent in FOKN (i.e. the omission of hydrodynamic and inverse Compton energy losses) greatly favor such detonation modes. As applied to the problem of atmospheric detonation, the code considers 5 particle species: ^{14}N, ^{4}He, ^{20}Ne, $^{10}X_7$, and electrons. Here $^{10}X_7$ is a hypothetical nuclei with an atomic weight of 10 and a Z of 7, two of which mock up the effects of a ^{20}Ne nucleus in terms of mass and radiative emission (which scales as Z^2). In addition to Coulomb scattering between all

species, the ^{14}N-^{14}N fusion reaction (26) is included, as well as an exceedingly generous representation of the fusion chain (36)-(40), given by:

$$\alpha + {}^{14}N \rightarrow {}^{10}X_7 + 2\alpha + 3.95 \text{ MeV} \qquad (42)$$

The cross sections assumed for these reactions are the measurements, upper limits, and/or fits for the $^{14}N + {}^{14}N$ fusion and $^{14}N(\alpha,p)^{17}O$ reactions given in Figs. 2 and 3, except that the rate for reaction (42) is multiplied by a factor of 1.5×10^{-2} to take into account the upper limit per-step-loss factors derived in Section VI.

Four cases were studied, in which the model atmosphere was subjected to conditions much more extreme than would result from any conceivable nuclear bomb explosion. In Case I, an atmospheric density nitrogen plasma ($n_i = 2.55 \times 10^{19}$ cm^{-3}) with $T_e = T_i = 10$ keV (initially) was bombarded with an equal number of 3.8 MeV α particles injected into it in 10^{-8} seconds. Case II was the same, except that the α energy and electron temperature were more realistically taken to be 2.6 MeV and 100 keV respectively. In Case III, no α's were injected and the atmospheric density nitrogen plasma initially had $T_i = 853$ keV and $T_e = 139$ keV, the maximum temperatures consistent with thermal steady state between electrons and ions even if all of the ^{14}N were burned (see Section IV). To test the effects of an initial state contrived to be far from steady state, the extreme case of an atmospheric density nitrogen plasma with $T_i = 2.5$ MeV and $T_e = 10$ keV (initially) was studied as Case IV.

In all cases, the nitrogen plasma was very rapidly cooled (in times $< 10^{-5}$ sec) by radiation losses, and no divergent fusion chain effects were

observed. The temperature and energy generation time history of Case IV is shown in Fig. 6. In no case did the nuclear reactions occurring in the cooling plasma come within a factor of 2900 of achieving breakeven, i.e., of equaling the energy originally present or injected into the plasma, as required by condition (2). Specifically, the energies produced in the four cases were 2.4×10^{-5}, 1.1×10^{-5}, 8.9×10^{-7}, and 3.4×10^{-4}, respectively, of that required for breakeven. The inclusion of the hydrodynamic and inverse Compton effects omitted by FOKN, would, in most cases, lower these results by more than an order of magnitude. It would be non-physical to run cases more energetic than these, because not enough nuclear energy is potentially available from the plasma to produce any higher internal energies.

Finally, although the velocity spectra of the fusion-product ions did deviate significantly from a Maxwellian distribution in these runs, as expected, the ^{14}N distribution remained very closely Maxwellian.

In general, the only deviation of the electron spectrum from Maxwellian was a very slight (2-7%) depression of the low energy tail due to their selective up-scattering by the more energetic ions, as expected from previous work.[37,38,41] The only exceptions to this behavior were transients occurring in the first 10^{-8}-10^{-7} seconds of Cases I and II, due to the co-injection of electrons with the alpha particles to maintain charge neutrality, and of Case IV, due to huge initial mismatch between electron and ion temperatures. These deviations were too small and/or short-lived to significantly affect the nuclear energy generated.

VIII. PROSPECTS FOR THE NUCLEAR DETONATION OF THE OCEANS

Non-equilibrium or fusion chain-mediated detonations of the Earth's oceans can be immediately ruled out because there are no exothermic reactions between their principal components which have Q $\langle\sigma v\rangle$'s at all comparable to those for radiative emission, even at the highest temperatures that could be reached if such reactions went to completion. Specifically, 1) p+p reactions are mediated only by the weak interaction;[21] 2) the $^{16}O(p,\gamma)^{17}F$ reaction has a cross section of only $\sim$15 microbarns above its Coulomb barrier[43] and ^{16}O+p reactions producing charged particles are endothermic by several MeV;[44] and 3) $O^{16}+O^{16}$ reactions have reaction rates and Q values[21] considerably smaller than those for $^{14}N+^{14}N$. Thus despite the fact that the effective Z of the ocean is a factor of 1.55 below that of the atmosphere, bremsstrahlung radiation losses still dominate nuclear energy generation by a very large margin, even when isotopic and other impurities are considered.

The prospects for initiating a propagating equilibrium thermonuclear detonation are relatively much more promising for the ocean than for the atmosphere, a priori, as the Coulomb barrier for proton-oxygen reactions is much lower than for nitrogen-nitrogen or helium-nitrogen ones, and because the medium is much more dense, implying that higher equilibrium temperatures may be attained (see Sections II and III). Also, the ocean contains 0.016% deuterium by number relative to hydrogen, as well as 0.03% and 0.2% of ^{17}O and ^{18}O, respectively, relative to ^{16}O, all of which may undergo exothermic, charged-particle-producing reactions with protons.

As was discussed in Section V, the propagation of an equilibrium detonation wave requires $t_{burn} \lesssim t_{hydro}$. t_{hydro} can be written in the form (for a plasma in equilibrium at temperature T, in keV):

$$t_{hydro} \simeq \frac{\ell}{c_s} = \ell\left(\frac{\rho}{\gamma P}\right)^{1/2} \qquad (43)$$

$$= \begin{cases} \dfrac{\ell}{4.0\times10^{7}} \left(\dfrac{\bar{A}}{T}\right)^{1/2} \text{ sec} & \text{if matter pressure dominates} \\ \dfrac{\ell}{7.8\times10^{6}} \dfrac{\rho^{1/2}}{T^{2}} \text{ sec} & \text{if radiation pressure dominates} \end{cases}$$

where ℓ is the characteristic detonation dimension in cm, $\bar{A}$ is the average atomic weight per particle (including electrons), and ρ is in g/cm^3.

From (3) we see that radiation pressure exceeds matter pressure when:

$$T > \left(\frac{3N_A\rho k}{\bar{A}a}\right)^{1/3} = 2.76\left(\frac{\rho}{\bar{A}}\right)^{1/3} \text{ keV} \qquad (44)$$

If all the ^{16}O in the ocean burned with the hydrogen [via the reactions $^{16}O(p,\gamma)^{17}F$ (Q = 0.60 MeV) and $^{17}F(p,\gamma)^{18}Ne$ (Q = 3.92 MeV), where we have neglected the beta decay of the ^{17}F ($t_{1/2}$ = 66 sec) due to the short hydrodynamic times involved (see below)], then an equilibrium temperature of 7.7 keV would be reached (where we have taken the detonating region to be two-fold compressed[5] so that ρ = 2 g/cm^3). At this temperature, we find, using (30) and reference 21, that t_{burn} (^{16}O) $\simeq 1.2\times10^{8}$ sec $\simeq$ 4 years. On the other hand, for $\ell = 10^6$ cm, corresponding to an ocean depth of 10 km, we find $t_{hydro} = 3\times10^{-3}$ sec. Thus, by the criterion (30) the oceans would fail to detonate via ^{16}O-burning by a factor of 4×10^{10}!

Burning all of the ^{18}O in the ocean [via the reactions $^{18}O(p,\alpha)^{15}N$ (Q = 3.98 MeV) and $^{15}N(p,\alpha)^{12}C$ (Q = 4.966 MeV)] would suffice to raise its

temperature to $\simeq$ 0.87 keV at ρ = 2 g/cm^3, corresponding to a nuclear burn time of 1.0×10^{18} sec and a hydrodynamic time of 3.1×10^{-2} sec. Thus ^{18}O burning fails to propagate by a factor of 3×10^{19}.

Similarly burning all the deuterium in the ocean [via the reaction $^{2}H(p,\gamma)^{3}He$ (Q = 5.494 MeV)] would raise its temperature to 0.094 keV at ρ = 2 g/cm^3, yielding $t_{burn} = 1.1\times10^{11}$ sec and $t_{hydro} = 9.4\times10^{-2}$ sec, for a safety margin of 1.2×10^{12}.

Similar calculations for other minor oceanic constituents (such as ^{12}C), show that their nuclear burn rates are too slow by at least as many orders of magnitude to maintain a nuclear detonation.

We therefore conclude that thermonuclear detonation waves cannot propagate in the terrestrial ocean by any mechanism, by an astronomically large margin.

It is worth noting in conclusion that the susceptability to thermonuclear detonation of a large body of hydrogenous material is an exceedingly sensitive function of its isotopic composition, and specifically to the deuterium atom-fraction, as is implicit in the discussion just preceding. If, for instance, the terrestrial oceans contained deuterium at any atom-fraction greater than 1:300 (instead of the actual value of 1:6000), the ocean could propagate an equilibrium thermonuclear detonation wave at a temperature $\gtrsim$ 2 keV (although a fantastic 10^{30} ergs—2×10^{7} MT, or the total amount of solar energy incident on the Earth for a 2 week period—would be required to initiate such a detonation at a deuterium concentration of 1:300). Now a non-negligible fraction of the matter in our own galaxy exists at temperatures much less than 300°K, i.e. the gas giant planets of our stellar system, nebulae, etc. Furthermore, it is well-known that thermodynamically-governed isotopic fractionation ever more strongly favors higher relative concentration of deuterium as the

temperature decreases, e.g. the D:H concentration ratio in the $\sim 10^{2}$°K Orion Nebula is about 1:200.[45] Finally, orbital velocities of matter about the galactic center of mass are of the order of 3×10^{7} cm/sec at our distance from the galactic core.

It is thus quite conceivable that hydrogenous matter (e.g. CH_4, NH_3, H_2O, or just H_2) relatively rich in deuterium ($\gtrsim$ 1 atom-%) could accumulate at its normal, zero pressure density in substantial thicknesses or planetary surfaces, and such layering might even be a fairly common feature of the colder, gas giant planets. If thereby highly enriched in deuterium ($\gtrsim$ 10 atom-%) thermonuclear detonation of such layers could be initiated artificially with attainable nuclear explosives. Even with deuterium atom fractions approaching 0.3 atom-% (less than that observed over multi-parsec scales in Orion), however, such layers might be initiated into propagating thermonuclear detonation by impact of large (diameter $\gtrsim 10^{2}$ meters), ultra-high velocity ($v \gtrsim 3 \times 10^{7}$ cm/sec) meteors or comets originating from nearer the galactic center. Such events, though exceedingly rare, would be spectacularly visible on distance scales of many parsecs.

IX. SUMMARY AND CONCLUSIONS

We have analyzed the general conditions for the initiation and propagation of nuclear detonation waves of both the equilibrium and non-equilibrium varieties in plane symmetry, e.g. layered media. We specifically find that neither the Earth's atmosphere nor its ocean can propagate any type of nuclear detonation, by very large margins. We have considered the possibility of fusion chain reactions and other non-thermal plasma phenomena, and found them of negligible importance.

In particular, we have shown that:

1. Even if nitrogen were many times as reactive as DT, the most reactive known fuel, the thermonuclear energy generation rate of the terrestrial atmosphere at <u>any</u> temperature would still not suffice to overcome the energy losses due to bremsstrahlung radiation and the inverse Compton effect.
2. Such high nuclear reactivities for nitrogen are precluded by basic physical laws governing the electrostatic repulsion of charged nuclei and the level density and parameters of nuclear energy states, as well as by experimental measurements.
3. Energy lost to radiation cannot be utilized to initiate further nuclear reactions, because the huge heat capacity of the radiation field at atmospheric density results in a sufficiently low equilibrium temperature ($\lesssim$ 1.4 keV) that the electrostatic repulsion between nuclei prevents <u>any</u> ^{14}N-^{14}N reactions at all from occurring by an astronomically large factor ($\sim 10^{145}$).
4. The fusion chain reactions proposed by McNally fail not only due to the rapid slowing of the suggested chain centers by Coulomb drag,

but also because of side reactions which absorb such chain centers, thereby precluding any possibility of a chain reaction.

5. Detailed non-thermal nuclear burn calculations were made in which the reactants, products, and electrons were not assumed to have Maxwellian velocity distributions, the kinematics and radiative emission were treated in a relativistically correct fashion, and separate Coulomb logarithms were calculated for each pair of interacting particles. These calculations included both $^{14}N + {}^{14}N$ fusion reactions and the "most dangerous" fusion chain ($2\alpha + 2{}^{14}N \rightarrow {}^{20}N + 4\alpha + 7.9$ MeV), assuming the highest physically possible reaction rates. Even at multi-MeV temperatures, no divergent chain effects occurred, the total nuclear energy generated always fell far below the input energy, and the material was always rapidly cooled by radiation losses in $< 10^{-5}$ seconds.
6. Similar considerations preclude the detonation of oceans of terrestrial composition, while admitting the possibility of detonating layers of suitable isotopic composition, density and depth on planetary (and possibly stellar) surfaces.

Acknowledgments

We wish to thank Edward Teller, Eugene Wigner and Gregory Breit for discussions of these matters and for encouragement to publish these results. We are particularly indebted to Roland Dayras and Z. E. Switkowski for communicating data on $^{14}N + {}^{14}N$ fusion reactions prior to publication, and to Stan Woosley and Robert Howerton for useful discussions on nuclear cross sections. We also express our appreciation to John Nuckolls for many useful background discussions.

REFERENCES

1. E. J. Konopinski, C. Marvin, and E. Teller, "Ignition of the Atmosphere with Nuclear Bombs", LA-602, LASL (1946); E. J. Konopinski and E. Teller, LA-001 LASL (1943).
2. H. A. Bethe, Bull. Atomic Scientists, 1, 2 (1946).
3. G. Breit, "Atmospheric Ignition", YALE (LA)-1 (1953).
4. Ya. B. Zel'dovich and Yu. P. Raizer, Physics of Shock Waves and High Temperature Hydrodynamic Phenomena (Academic Press, New York, 1966).
5. Ya. B. Zel'dovich and A.S. Kompaneets, Theory of Detonation (Academic Press, New York, 1960).
6. W. D. Arnett, Astrophys. Space. Sci. 5, 180 (1969).
7. S. W. Bruenn and A. Marroquin, Ap. J. 195, 567 (1975).
8. J. H. Mahaffy and C. J. Hansen, Ap. J. 201, 695 (1975).
9. M. S. Chu, Phys. Fluids 15, 413 (1972).
10. E. Teller, "Concerning Strong Convergent Compression of Thermonuclear Fuel in Laser-Fusion CTR Schemes", UCRL-74117 (1972).
11. G. B. Zimmerman, "Numerical Simulation of the High-Density Approach to Laser Fusion", UCRL-74811 (1973).
12. Laser Program Annual Report-1974, Lawrence Livermore Laboratory, UCRL-50021-74 (1975), p. 368-423.
13. J. Nuckolls, "Laser-Induced Implosion and Thermonuclear Burn", in Laser Interactions and Related Plasma Phenomena, Vol. 3, ed. H. Schwartz and H. Hora (Plenum Press, New York, 1974).
14. S. Maxon, Phys. Rev. A5, 1630 (1972).
15. G. Cooper, Phys. Rev. D3, 2312 (1971).
16. S. A. Colgate, Ap. J. 187, 321 (1974).

17. T. A. Weaver and G. F. Chapline, Ap. J. (Letters) 192, L57 (1974); T. A. Weaver, Ap. J. Suppl. 32, 233 (1976).
18. M. L. Alme and J. R. Wilson, Ap. J. 186, 1015 (1974).
19. S. L. Shapiro and E. E. Salpeter, Ap. J. 198, 671 (1975).
20. A. M. Lane and G. Thomas, Rev. Mod. Phys. 30, 257 (1958).
21. W. A. Fowler, G. R. Caughlan, and B. A. Zimmerman, Ann. Rev. Astro. Astrophys. 13, 69 (1975).
22. S. E. Woosley, W. A. Fowler, J. A. Holmes, and B. A. Zimmerman, "Tables of Thermonuclear Reaction Rate Data for Intermediate Mass Nuclei" Caltech OAP-422 (1975).
23. Z. E. Switkowski, R. G. Stokstad, and R. M. Wieland, Nucl. Phys. A274, 202 (1976).
24. C. Y. Wong, Phys. Rev. Lett. 31, 766 (1973); R. Dayras, private communication (1976).
25. N. P. Heydenburg and G. M. Temmer, Phys. Rev. 92, 89 (1953).
26. E. Kashy, P. D. Miller, and J. R. Risser, Phys. Rev. 112, 547 (1958); D. G. Herring, R. Chiba, B. R. Gasten, and H. T. Richards, Phys. Rev. 112, 1210 (1958).
27. H. Yamaguchi, et al., Institute for Nuclear Study Report INSJ-35, University of Tokyo (1960).
28. T. A. Tombrello, Proc. Conf. on Nuclear Cross Sections and Technology, Washington, D.C., March 1975, ed. C. D. Bowman and R. A. Schrack (American Nuclear Society, Springfield, Va. NTIS COM-75-11469), p. 659.
29. D. D. Clayton, Principles of Stellar Evolution and Nucleosynthesis (McGraw-Hill, New York, 1968).
30. L. Spitzer, Physics of Fully Ionized Gases (Interscience, New York, 1962).
31. G. Cooper and K. Nishimura, "Relativistic and Velocity Dependent Effects for Electron-Ion Coupling in a Plasma", UCIR-564 (LLL, 1971).

32. A. P. Porter, T. A. Weaver, G. B. Zimmerman, J. H. Nuckolls, E. Teller, and L. Wood, "Performance Parameters of Thermonuclear Fuels in Laser-Compressed and -Ignited Pellets", Bull. APS 18, 1300 (1973), and UCRL-74958 (1973).
33. U. Jetter, Physik. Blatt. 6, 199 (1950); ORNL-TR-842.
34. J. R. McNally, Jr., Nuclear Fusion 11, 187, 189, 191, 554 (1971).
35. J. R. McNally, Jr., Nuclear Data in Science and Technology 2, 41 (1973); J. R. McNally, Jr., "Ignition of the Atmosphere with Nuclear Bombs", preprint (1975).
36. T. Weaver, G. Zimmerman, and L. Wood, "$B^{11}(p, 2\alpha)He^4$: A Clean, High Performance CTR Fuel", UCRL-74352 (LLL, 1972).
37. T. Weaver, G. Zimmerman, and L. Wood, "Exotic CTR Fuels: Non-Thermal Effects and Laser Fusion Applications", Bull. APS 18, 1300 (1973), and UCRL-74938 (LLL, 1973).
38. T. C. Chu, "Effects of Cyclotron Radiation in Magnetically Confined p-^{11}B Reactors", Bull. APS 20, 1317 (1975), and UCRL-77167 (LLL, 1975).
39. E. F. Plechaty, D. E. Cullen, R. J. Howerton, and J. R. Kimlinger, "Tabular and Graphical Representation of 175 Neutron Group Constants Derived from the LLL Evaluated Neutron Data Library (ENDL)", UCRL-50400, Vol. 16 (LLL, 1975); D. E. Cullen, R. C. Haight, R. J. Howerton, M. H. MacGregor and S. T. Perkins, "Graphical, Experimental Data for Major Neutron Induced Reactions ($Z \leq 55$)", UCRL-50400, Vol. 7A (LLL, 1974).
40. J. K. Blair and F. X. Haas, Phys. Rev. C7, 1356 (1973).
41. G. Lee, G. Zimmerman, and L. Wood, "Concerning Electron-Ion Coupling and Charged Particle Energy Deposition During Vigorous Thermonuclear Burn", UCRL-74192 (LLL, 1972).

42. G. B. Zimmerman, T. Scharkmann, L. Wood, T. Weaver, T. Chu, and G. Lee, "FOKN: A Relativistic Fokker-Planck Code with Large Angle Scattering and Radiation Losses", UCID-17196 (LLL, 1976).

43. J. J. Domingo, Nucl. Phys. 61, 39 (1965).

44. F. Ajzenberg-Selove, Nucl. Phys. A166, 1 (1971).

45. K. B. Jefferts, A. A. Penzias, and R. W. Wilson, Ap. J. Lett. 179, L457 (1973).

NOTICE

"This report was prepared as an account of work sponsored by the United States Government. Neither the United States nor the United States Department of Energy, nor any of their employees, nor any of their contractors, subcontractors, or their employees, makes any warranty, express or implied, or assumes any legal liability or responsibility for the accuracy, completeness or usefulness of any information, apparatus, product or process disclosed, or represents that its use would not infringe privately-owned rights."

Reference to a company or product name does not imply approval or recommendation of the product by the University of California or the U.S. Department of Energy to the exclusion of others that may be suitable.

FIGURE CAPTIONS

Figure 1. Experimental (solid line and points) and extrapolated (dashed lines) cross sections for $^{14}N + {}^{14}N$ fusion as a function of the laboratory energy of the bombarding ^{14}N nucleus.

Figure 2. Experimental (σ_{EXPT}) and adopted (σ_{ADPT}) cross sections for the $^{14}N(\alpha,p)^{17}O$ reaction as a function of laboratory energy of the bombarding α particle.

Figure 3. Relativistic correction factors and other parameters related to electron-ion temperature balance for the case of the Earth's atmosphere.

Figure 4. The rate of bremsstrahlung energy loss, $\dot{E}_{BREM}$, in a plasma of atmospheric density and composition, compared with an upper limit to its rate of nuclear energy generation, $\dot{E}_N$, as a function of the ion temperature, T_i. $T_{i,max}$ is the largest steady-state ion temperature that could be reached if all the nitrogen in the plasma were burned to ^{20}Ne via reaction (26).

Figure 5. The experimental cross section, σ_{EXPT}, for the $^{11}B(p,2\alpha)^4He$ reaction, compared with the proton stopping cross section due to Coulomb friction with a background nitrogen plasma, σ^C_{pN}, as a function of E_p, the laboratory energy of the bombarding proton.

Figure 6. Time evolution of the ^{14}N and electron temperatures (T_N and T_e respectively) for a 2.55×10^{19} cm^{-3} nitrogen plasma, started at t = 0 with T_N = 2.5 MeV and T_e = 10 keV (Case IV). Also shown is the fraction of breakeven represented by the nuclear energy generated (right hand scale). The plasma is assumed to be perfectly confined, with bremsstrahlung radiation emission being the only energy loss.

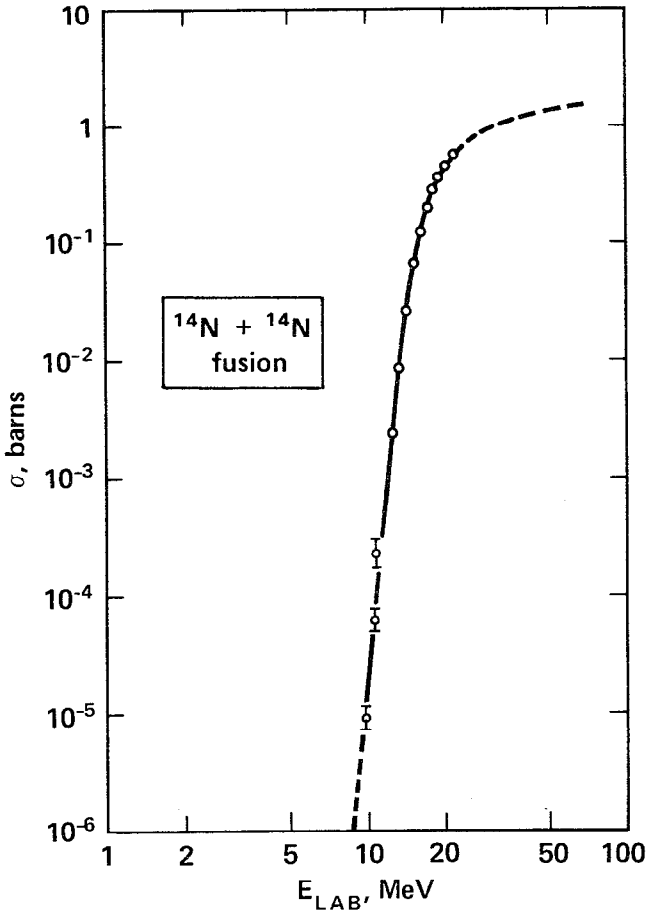


Figure 1

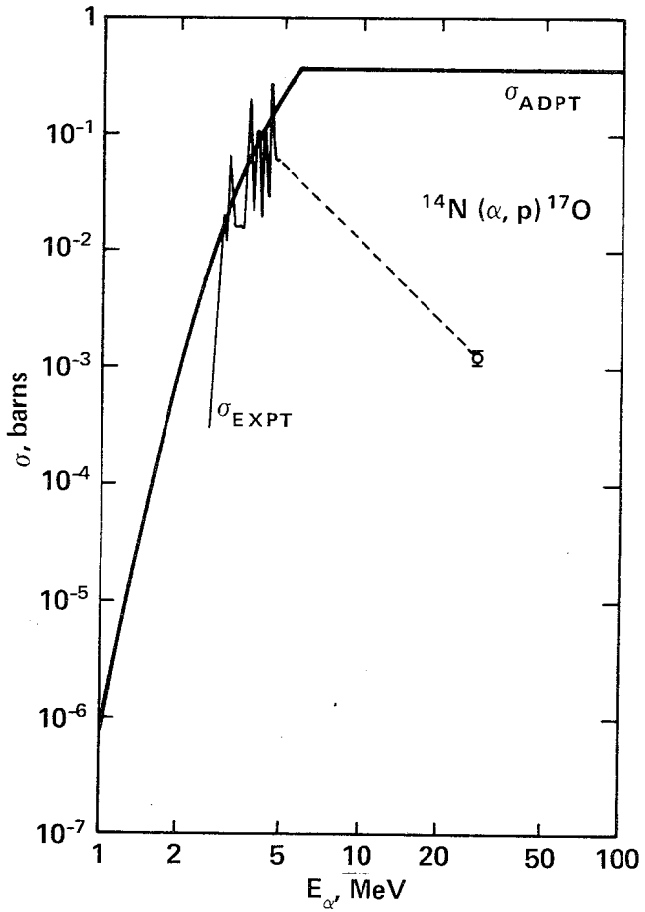


FIGURE 2

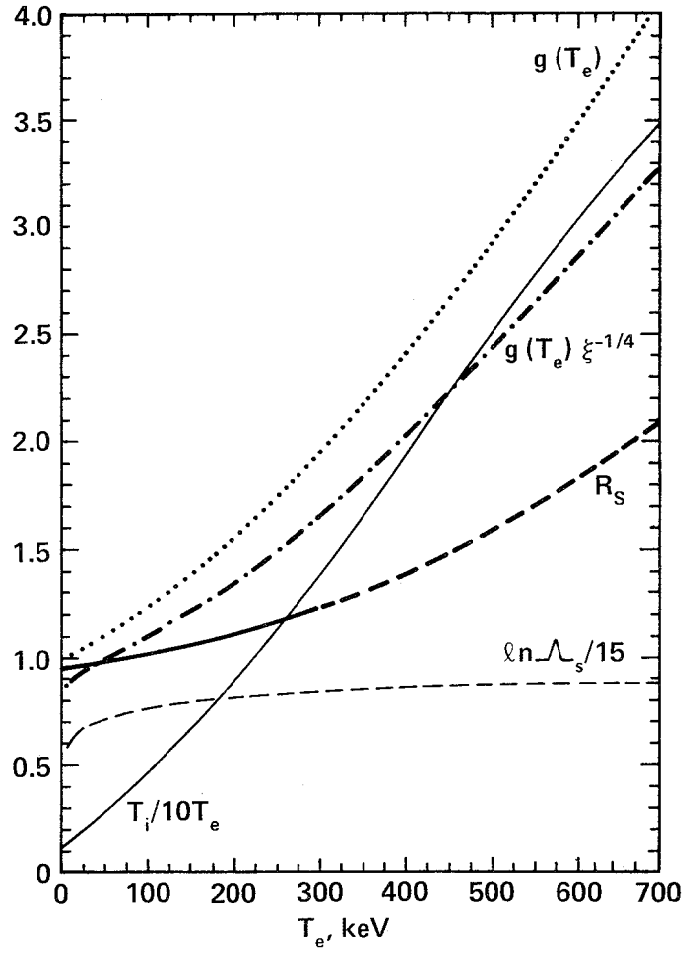


FIGURE 3

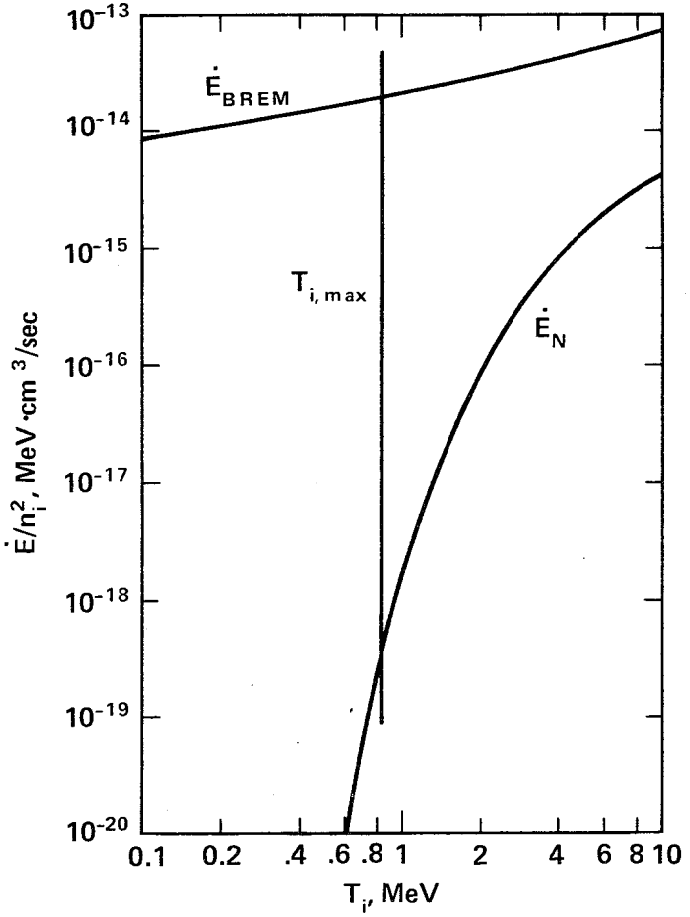


Figure 4

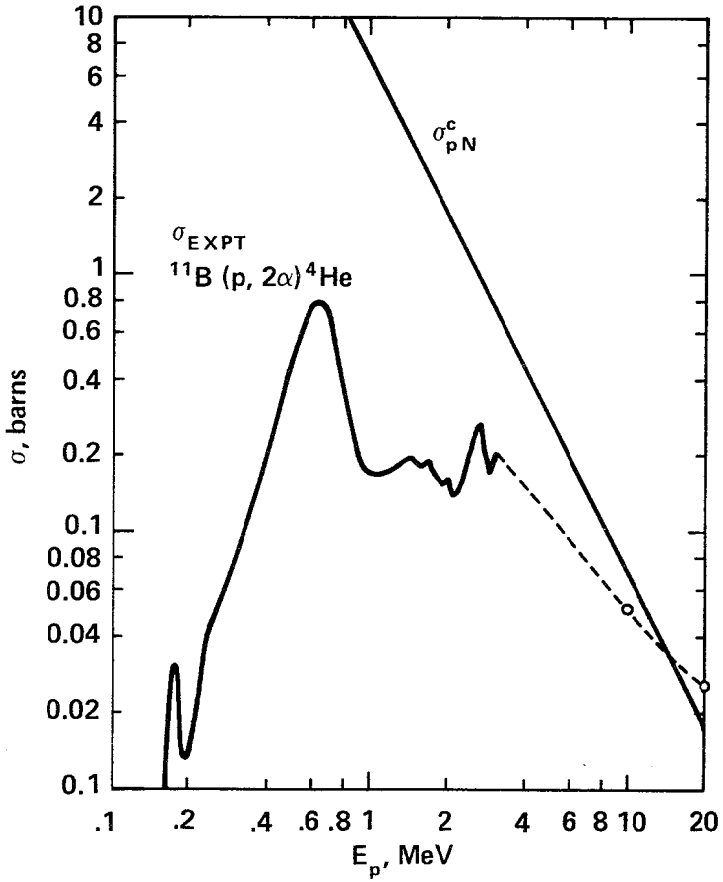


Figure 5

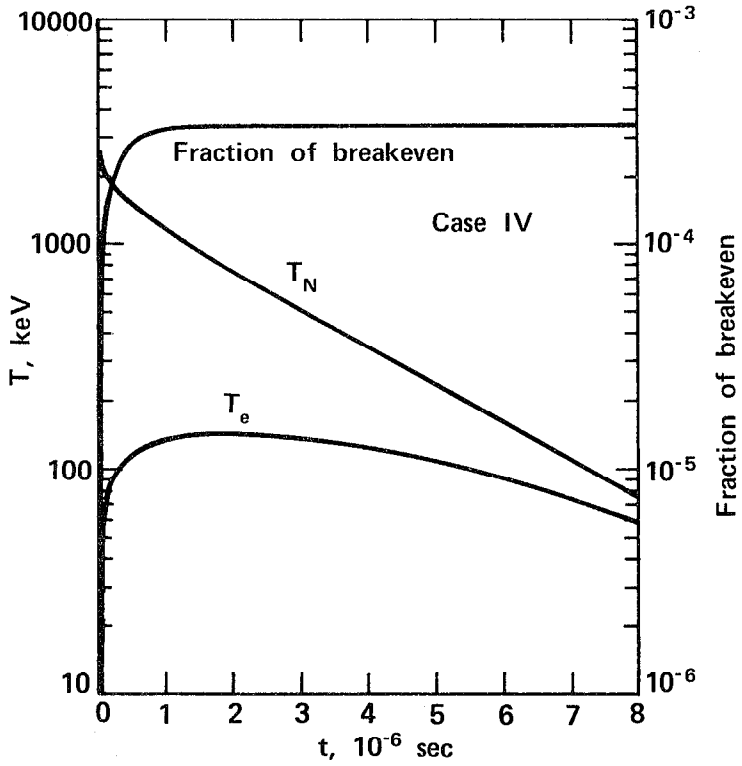

10000
1000
100
10
T, keV
Fraction of breakeven
Case IV
T_N
T_e
0
1
2
3
4
5
6
7
8
t, 10^{-6} sec
10^{-3}
10^{-4}
10^{-5}
10^{-6}
Fraction of breakeven

Figure 6